

1. NO CALCULATORS ALLOWED
2. UNLESS STATED OTHERWISE, YOU MUST SIMPLIFY ALL ANSWERS
3. SHOW PROPER CALCULUS LEVEL WORK TO JUSTIFY YOUR ANSWERS

The graph of f is shown on the right. Evaluate the following limits. Write "DNE" if a limit does not exist.

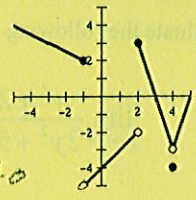
SCORE: 0 / 3 PTS

[a] $\lim_{x \rightarrow 4} \frac{3x}{5-f(x)}$ $f(x) = -4$

$$\lim_{x \rightarrow 4} \frac{3x}{5-f(x)} = \lim_{x \rightarrow 4} \frac{3x}{1} = 12$$

[b] $\lim_{x \rightarrow -1^+} f(x)$ DNE

The right hand limit $\neq$ to the Left hand limit



Prove that $\lim_{x \rightarrow 0} x^6 \cos \frac{1}{x^3} = 0$. by using squeeze theorem

SCORE: 2.5 / 3 PTS

$$\lim_{x \rightarrow 0} x^6 \lim_{x \rightarrow 0} \cos \frac{1}{x^3}$$

$$\lim_{x \rightarrow 0} x^6 = 0^6 = 0 \quad \textcircled{\frac{1}{2}}$$

$$-1 \leq \cos \frac{1}{x^3} \leq 1$$

by multiplying x^6

$$-x^6 \leq x^6 \cos \frac{1}{x^3} \leq x^6 \quad \textcircled{1}$$

by applying the limit to both sides

$$0 \leq x^6 \cos \frac{1}{x^3} \leq 0$$

According to squeeze theorem

$x^6 \cos \frac{1}{x^3}$ is zero

$$\lim_{x \rightarrow 0} x^6 \cos \frac{1}{x^3} = 0 \quad \checkmark$$

1

If $\lim_{r \rightarrow -1} \frac{4+ar-r^6}{1+r}$ exists, find the value of a .

$f(-1)$ for $4+ar-r^6$ should be 0 so the limit will exist

SCORE: 2 / 2 PTS

$$4 - a - 1 = 0 \quad \textcircled{1}$$

$$-a = -3$$

$$a = 3 \quad \textcircled{1}$$

$$\lim_{x \rightarrow -1} \frac{4+3x-x^6}{1+x}$$

Using complete sentences and proper mathematical notation, write the formal definition of "vertical asymptote". SCORE: 0 / 2 PTS

vertical asymptote: The vertical asymptote is an imaginary line where the graph of a certain function $f(x)$ will never intersect with or will never cross it.

~~PARALLEL - SO NEVER CROSSES - VERTICAL ASYMPT?~~

Evaluate the following limits. Write "DNE" if a limit does not exist.

SCORE: 4 1/2 / 7 PTS

[a] $\lim_{y \rightarrow -4} \frac{y^2 + 2y - 8}{2y^2 + 5y - 12}$ $(y+4)(y-2)$

$$= \lim_{y \rightarrow -4} \frac{(y+4)(y-2)}{(2y-3)(y+4)}$$

$$= \lim_{y \rightarrow -4} \frac{y-2}{2y-3} \quad (1)$$

$$= \frac{-4-2}{-8-3}$$

$$= \frac{-6}{-11} = \frac{6}{11}$$

[c] $\lim_{t \rightarrow -5} \frac{t-1}{t^2+25} = \frac{6}{-6} - \frac{4^2}{-2}$

$$= \frac{-1-2}{50} = \boxed{\frac{-3}{50}}$$

[b] $\lim_{b \rightarrow 3} \frac{b - \sqrt{b+6}}{6-2b} \times \frac{b + \sqrt{b+6}}{b + \sqrt{b+6}}$

$$\lim_{b \rightarrow 3} \frac{b^2 - b + 6}{6-2b(b + \sqrt{b+6})} \times \frac{-2}{-2}$$

$$\lim_{b \rightarrow 3} \frac{(b-3)(b+2)}{6-2b(b + \sqrt{b+6})}$$

$$\lim_{b \rightarrow 3} \frac{(b+2)}{-2(b + \sqrt{b+6})} \quad (1)$$

$$= \frac{3+2}{-2(3+3)} = \boxed{\frac{5}{-12}} \quad (\frac{1}{2})$$

[d] $\lim_{x \rightarrow -2} f(x)$ where $f(x) = \begin{cases} 2x+1, & \text{if } x < -2 \\ x-1, & \text{if } -2 < x < 3 \\ 5-x, & \text{if } x > 3 \end{cases}$

$$\lim_{x \rightarrow -2^-} 2x+1 = -3 \quad (\frac{1}{2})$$

$$\lim_{x \rightarrow -2^+} x-1 = -3 \quad (\frac{1}{2})$$

$$\lim_{x \rightarrow -2} f(x) = -3 \quad (1)$$

because Left side limit = Right side limit